# Modifiers of Modal Auxiliaries: New Sources for Ordering Sources

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LSA 2013 Annual Meeting Boston, MA Jan. 5, 2013

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### Modifying Modals

- Modifiers of modal auxiliaries (MMAs) have not yet been given a formal compositional account.
- The vase could easily fall. (1)
- The effect of the MMA in (1) is to strengthen or intensify a modal.
- The vase could easily fall.  $\rightarrow$  The vase could fall. (2)
  - The vase could fall.  $\rightarrow$  The vase could easily fall.
- Note that this is not the same *easily* as in (3), which could be paraphrased as "with ease"; this use of *easily* requires an agentive verb, which is not present in (2)
- He could easily lift it over his head.  $\leftrightarrow$  He could lift it over his head with ease. (3)b. The vase could easily fall.  $\leftrightarrow$  #The vase could fall with ease.
- Recent work has shown that at least some modals, like *likely*, are gradable (Yalcin 2007, 2010; Lassiter 2011; Klecha 2012), requiring a modal semantics which is compatible with a Kennedystyle semantics for gradability (Kennedy 1999, 2007; Kennedy and McNally 2005), which allows for the combination of gradable modals with degree modifiers like *more*, too, very, etc.
- Lassiter (2011) argues in light of this that all modals, even modal auxiliaries, are inherently scalar; so maybe *easily* is like a degree modifier?
- a. [[likely]]<sub>Lassiter</sub> =  $\lambda p[Pr(p)]$ b. [[could]]<sub>Lassiter</sub> =  $\lambda p[Pr(p) \succ 0]$ (4)
- But *could* cannot combine with degree modifiers more generally, and *easily* does not combine with anything other than modal auxiliaries.
- Yalcin (2007) argues for a mixed account where some modals are gradable and some have a traditional quantificational semantics; moreover, Klecha (2012a, in progress) specifically rebuts Lassiter, arguing that modal auxiliaries may have a Kratzerian quantificational semantics.
- I propose a semantics for *easily* which allows for it to act as a "possibility intensifier" but without abandoning a Kratzerian quantificational semantics for possibility modals, as Lassiter (2011) does.
- Rather, *easily* restricts the domain of the modal, giving a stronger interpretation

## Gradability

- A first cut analysis might be that *easily* is an overt ordering source, which provides a more restrictive ordering
- The modal *could* then takes the best of the worlds in the modal base as determined by this ordering to return a more exclusive modal domain (say, only highly probable or stereotypical worlds)
- (5)  $[[\operatorname{could}]] = \lambda \phi[\lambda m[\lambda g[\lambda w[\exists v \in \operatorname{BEST}_{g(w)}(\cap m(w))[\phi(v)]]]]]$
- However, *easily* is itself gradable:
- The vase very easily could have fallen. (6)
  - The piggy bank fell, but the vase just as easily could have fallen.
- An ordering source is a set of propositions from which the modal determines an ordering and narrows its domain
- Klecha (2012a, in progress) argues that degree modification is the primary diagnostic for gradability, i.e., type  $\langle \alpha, \langle s, d \rangle \rangle$ ; given that *easily* combines with degree modifiers, *easily* must denote a measure function
- I argue that *easily* denotes a stereotypical ordering over worlds given an evaluation world
- Thus it is of type  $\langle s, \langle s, d \rangle \rangle$
- $[[easily]] = \lambda v [\lambda w [STEREOTYPICALITY(v)(w)]]$

#### Degree Modification

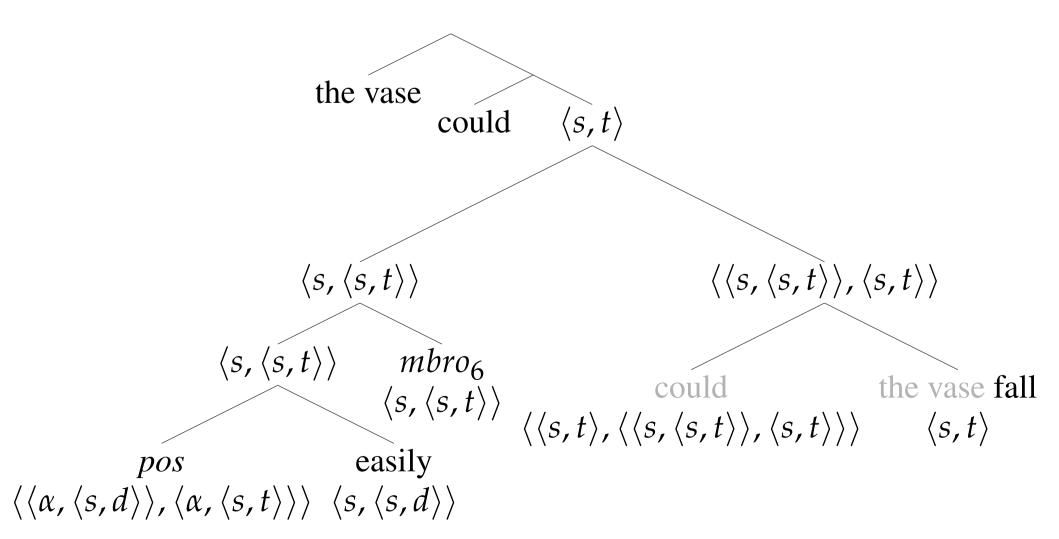
- I take degree modifiers to have the type  $\langle \langle \alpha, \langle s, d \rangle \rangle$ ,
- Already needed to account for adjective type variabi
- $\llbracket \text{tall} \rrbracket^g = \lambda x_e [\lambda w[\text{height}(x)(w))] \end{bmatrix}$ (8)  $\llbracket \text{just as}_7 \rrbracket^g = \lambda G_{\langle \alpha, \langle s, d \rangle \rangle} [\lambda x_{\alpha} [\lambda w [G(x)(w)$ [just as<sub>7</sub> tall] $g = \lambda x_e [\lambda w [height(x)(w) =$

 $[[early]]^g = \lambda x_{\epsilon} [\lambda w [earliness(x)(w)]]$  $\llbracket \text{just as}_7 \rrbracket^g = \lambda G_{\langle \alpha, \langle s, d \rangle \rangle} [\lambda x_\alpha [\lambda w [G(x)(w)$ [just as<sub>7</sub> early] $g = \lambda x_{\epsilon} [\lambda w]$  earliness(x)(w)

- This means that *easily* can also combine with degree
- $[[easily]]^g = \lambda v [\lambda w [STEREOTYPICALITY(v)]$ (9)  $\llbracket \text{just as}_7 \rrbracket^g = \lambda G_{\langle \alpha, \langle s, d \rangle \rangle} [\lambda x_{\alpha} [\lambda w [G(x)(w)$ [just as<sub>7</sub> easily] $g = \lambda v [\lambda w [ST(v)(w) = g(z)]$
- And with the positive morpheme, which relates the a standard relative to an anaphorically introduced c class (Kennedy 2007)
- $[[easily]]^g = \lambda v [\lambda w [ST(v)(w)]]$ (10) $\llbracket pos_8 \rrbracket^g = \lambda G_{\langle \alpha, \langle s, d \rangle \rangle} [\lambda x_{\alpha} [\lambda w [G(x)(w)$  $\llbracket pos_8 \text{ easily} \rrbracket^g = \lambda v [\lambda w [ST(v)(w) \succeq s(ST)(g(8))(w)]]$

### Compositional Analysis of MMAs

- The MMA *easily* attaches as the sister of *mbro*<sub>6</sub>; both are of type  $\langle s, \langle s, t \rangle \rangle$
- I assume they combine via a generalized Predicate Modification rule:
- both of type  $\langle \tau, \langle s, t \rangle \rangle$ , then let  $[\![\alpha]\!] = \lambda x_{\tau} [\lambda w[\![\beta]\!](x)(w) \& [\![\gamma]\!](x)(w)]\!]$ • Giving the following derivation:
- [the vase fall]  $g = \lambda w [tvf(w)]$
- $\llbracket \text{could} \rrbracket^{g} = \lambda \phi_{\langle s,t \rangle} [\lambda m_{\langle s,\langle s,t \rangle \rangle} [\lambda w [\exists v \in m(w) [\phi(v)]] ]$ [[the vase could fall]] $g = \lambda m_{\langle s, \langle s, t \rangle \rangle} [\lambda w [\exists v \in m(v)]]$  $\llbracket mbro_6 \rrbracket^g = \lambda v [\lambda w [v \in \cap g(6)(w)]]$
- $\llbracket pos_8 \text{ easily} \rrbracket^g = \lambda v [\lambda w [ST(v)(w) \succeq s(ST)(g(8))]$  $[pos_8 \text{ easily } mbro_6]^g =$
- $\lambda v[\lambda w[ST(v)(w) \succeq s(ST)(g(8))(w) \& v \in \cap g$ [[the vase could  $pos_8$  easily  $mbro_6$  fall]]g =
- $\lambda w[\exists v[\mathsf{ST}(v)(w) \succeq s(\mathsf{ST})(g(8))(w) \& v \in \cap g(6)(w) \& \mathsf{tvf}(v)]]$



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	Compositionality: Basics	Why
$(\alpha, \langle s, t \rangle)$ oility $(a, \langle s, t \rangle) = g(7) ]]]$	<ul> <li>Some assumptions about modal compositionality:</li> <li>The modal base is represented in the syntax</li> <li>I also assume the modal does <i>not</i> take a modal base argument directly (i.e., a set of propositions); rather it takes an accessibility relation</li> </ul>	•
g(7)]]	• The intersection of the modal base is accomplished by the modal base <i>pro</i> ( <i>mbro</i> ); this expression bears an index which is mapped by the assignment function to a function from a world to a set	
g(7)]]] g(7)]] g(7)]] e modifiers	<ul> <li>of propositions, i.e., a modal base</li> <li>Also contrary to much literature, I argue that <i>could</i> does not have an ordering source (more on this below)</li> </ul>	
(w)]]) = g(7)]]]	$\llbracket mbro_6 \rrbracket^g = \lambda v [\lambda w [v \in \cap g(6)(w)]]$ $\llbracket could \rrbracket^g = \lambda \phi_{\langle s,t \rangle} [\lambda m_{\langle s,\langle s,t \rangle \rangle} [\lambda w [\exists v \in m(w) [\phi(v)]]]]$ $\llbracket mbro_6 could \phi \rrbracket^g = \lambda w [\exists v \in \cap g(6)(w) [\phi(v)]]$	(12)
(7)]] the target to comparison	$\langle s, t \rangle$	(12)
<b>r</b>	$\begin{array}{l} mbro_{6} \\ \langle s, \langle s, t \rangle \rangle, \langle s, t \rangle \rangle \end{array}$	
$\succeq s(G)(g(8))$	$(w)]]]$ MOD $\phi$	Exclu

**Generalized Predicate Modification** If a node  $\alpha$  has two daughters,  $\beta$  and  $\gamma$ ,

	LEX
(v)]]]]	LEX
w)[tvf(v)]]]	FA
	LEX
))(w)]]	(10)
g(6)(w)]]	GPM

FA

### Context Sensitivity

 $\langle \langle s,t \rangle, \langle \langle s, \langle s,t \rangle \rangle, \langle s,t \rangle \rangle \rangle \langle s,t \rangle$ 

• Consider a conditional in conjunction with *easily*:

(13)

- Suppose that the antecedent unlikely; i.e., there are no stereotypical worlds with a strong gust • It looks like this gives us an empty modal base and fails to derive the right meaning
- The original lexicalized superlative semantics for ordering sources was formulated to get around this very problem (Kratzer 1981, 2012)
- But recall that *pos* crucially determines a standard of comparison contextually (Kennedy 2007) • As with attributive adjectives, the comparison class may come from its sister:

That is a tall {boy/man/skyscraper}. (14)

- Likewise, the standard of stereotypicality is relativized to which worlds are in the modal base • This provides an intriguing alternate strategy for dealing with various problems that the original formulation of the ordering source was meant to solve

Bonus: Can MMAs tell us about syntax of modals?

• Note that *easily*'s position is highly variable:

It (easily) could (easily) have (easily) fallen. (15)

- Can this tell us anything about the syntactic position of *could* a la quantifier float? • This might suggest that *could* starts below *have* in (15), which is consistent with the analysis in
- Condoravdi (2002)

#### no ordering source for *could*?

- uld lexically has no ordering source, how to exclude outsh worlds?
- na (2012b, in progress): exclusion of outlandish worlds is ecision, a pragmatic effect
- is because the exclusion of these worlds is **defeasible**, eas with *easily*, it is not
- A man walks along a tightrope between two buildings, secured by a safety line
- You could have fallen to your death!
- No, I couldn't have I had a safety line which was tested right beforehand.
- Yes, but the safety line could have broken in some unforseen way!
- A man walks along a tightrope between two buildings, secured by a safety line
- You could easily have fallen to your death!
- No, I couldn't have I had a safety line which was tested right beforehand.
- c. #Yes, but the safety line could have broken in some unforseen way!
- Exclusion of non-stereotypical worlds with just *could* is pragmatic; semantic with *easily*
- Other modals may have ordering sources lexically (e.g., deontics, teleologicals)

If a strong gust of wind had come along, you could easily have fallen.